

# The Xpult

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## Key Concepts

- Process capability
- Reduction of variability
- Design of experiments

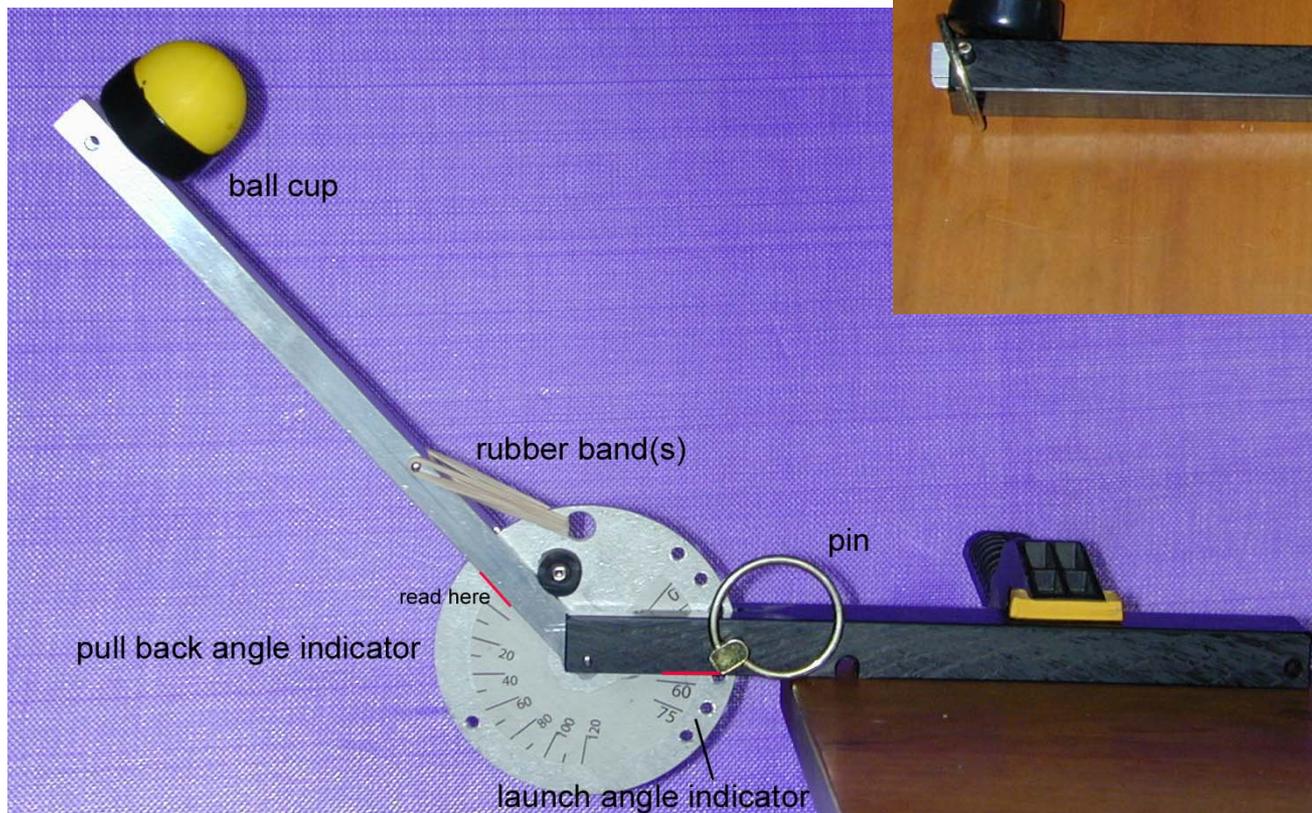
## Existing Devices

- We did not invent the idea of a catapult for teaching process control.
- Several existing devices.
- Big, heavy, expensive. (e.g., 5kg, \$400)



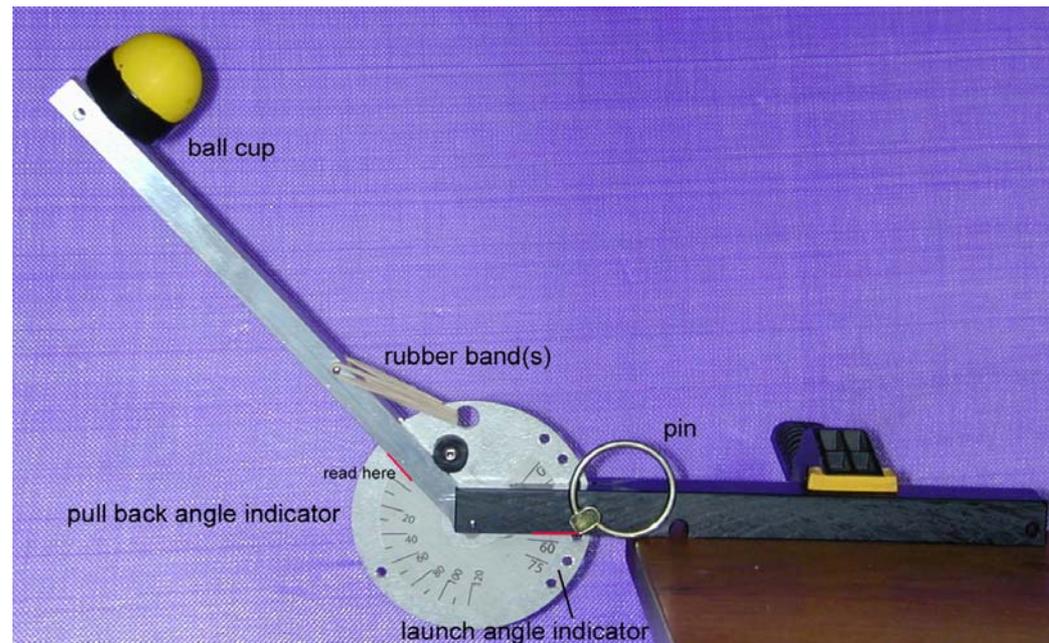
## Goal: A catapult for every student (or student team)

- Target price <\$25/kit.
- Small enough to fit in book bag.
- Eliminate obvious coupling of variables.



# Basic Operation

- Performance measures
  - Distance launched
  - Percentage of “baskets” made
  - Variance in distance
  - etc.
- Independent variables
  - Ball type: perforated or smooth
  - Number of rubber bands: 1, 2, 3
  - Launch angle: 0, 15, 30, 45, 60, 75, 90 degrees
  - Pull-back angle 0-120 degrees

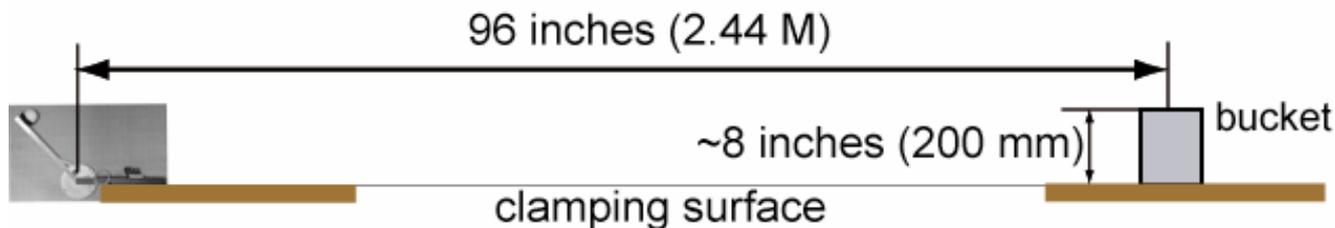


## Homework Exercise

1. Holding everything else constant, how do you expect the variables to influence distance?
  - a) When I increase the number of rubber bands, the launch distance \_\_\_\_\_.
  - b) When I increase the launch angle, the launch distance \_\_\_\_\_.
  - c) When I increase the pull back angle, the launch distance \_\_\_\_\_.
  - d) I expect the table tennis ball to go \_\_\_\_\_ than the perforated plastic ball.
2. Is there exactly one set of values that will result in launching a ball 96 inches?
3. If more than one set of values will work, why might you prefer one set to another?
4. For the ambitious, you might try plotting launch distance as a function of each of the four variables. If you do this, you probably want to hold the other three variables constant at “reasonable” values.

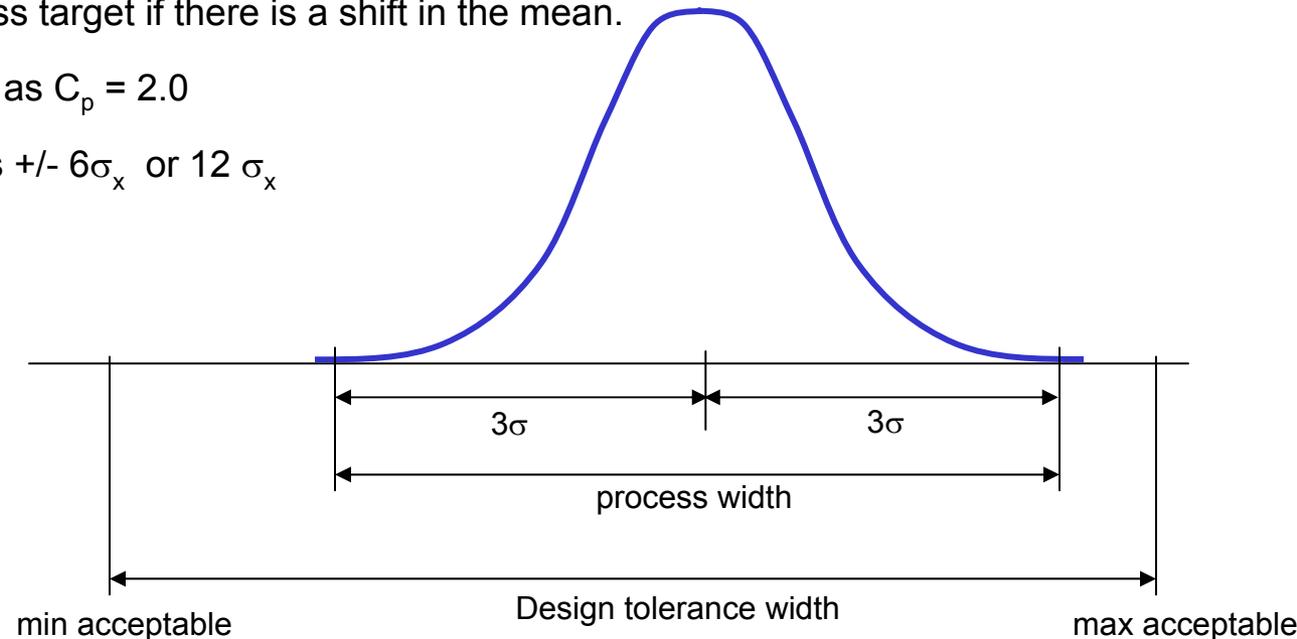
Objective:

Launch the ball into a bucket 96 inches from the catapult pivot, with the bucket opening 8 inches above the clamping surface.



# Process Capability

- $C_p = (\text{design tolerance width})/(\text{process width}) = (\text{max-spec} - \text{min-spec})/6\sigma_x$
- Example:
  - Plane is “on time” if it arrives between  $T - 15\text{min}$  and  $T + 15\text{min}$ .
  - Design tolerance width is therefore 30 minutes
  - $\sigma_x$  of arrival time is 12 min
  - $C_p = 30/6*12 = 30/72 = 0.42$
- A “capable” process can still miss target if there is a shift in the mean.
- Motorola “Six Sigma” is defined as  $C_p = 2.0$ 
  - I.e., design tolerance width is  $\pm 6\sigma_x$  or  $12\sigma_x$



- Put team settings on screen/board.
- Pick team to demo their settings.
- What are the possible causes of variability in launch distance?
- Define process capability (using different size targets)
- How can capability be increased?
- Basic idea of robustness.
- How might robust settings be found.

## Primary School Science and Math Education

- Catapult is popular with 6-12 year olds.
- Can be used to teach graphs, experimentation, scientific method, basic physics.
- Plan to “seed” several hundred units with math and science teachers.



## Further Information

Instructions can be downloaded at  
<http://opim.wharton.upenn.edu/~ulrich>

New chapter in Ulrich and Eppinger *Product Design and Development* 3rd Edition on “Robust Design.”

Contact Christian Terwiesch or Karl Ulrich for catapults:

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